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Effects of Low-Velocity Fault Damage Zones on Long-Term Earthquake Behaviors on Mature Strike-Slip Faults

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Key Points:
- Fully dynamic earthquake cycle simulations show persistent heterogeneous stress distribution generated by fault zone waves
- Faults surrounded by low-velocity damage zones lead to more complexities in earthquakelocation, size, and slip patterns
- Both lithology and rheology influence the depth distribution of seismicity, with shallow fault damage zones exhibiting bimodal distribution

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Abstract Mature strike-slip faults are usually surrounded by a narrow zone of damaged rocks characterized by low seismic wave velocities. Observations of earthquakes along such faults indicate that seismicity is highly concentrated within this fault damage zone. However, the long-term influence of the fault damage zone on complete earthquake cycles, that is, years to centuries, is not well understood. We simulate aseismic slip and dynamic earthquake rupture on a vertical strike-slip fault surrounded by a fault damage zone for a thousand-year timescale using fault zone material properties and geometries motivated by observations along major strike-slip faults. The fault damage zone is approximated asan elastic layer with lower shear wave velocity than the surrounding rock. We find that dynamic wave reflections, whose characteristics are strongly dependent on the width and the rigidity contrast of the fault damage zone, have a prominent effect on the stressing history of the fault. The presence of elastic damage can partially explain the variability in the earthquake sizes and hypocenter locations along a single fault, which vary with fault damage zone depth, width and rigidity contrast from the host rock. The depth extent of the fault damage zone has a pronounced effect on the earthquake hypocenter locations, and shallower fault damage zones favor shallower hypocenters with a bimodal distribution of seismicity along depth. Our findings also suggest significant effects on the hypocenter distribution when the fault damage zone penetrates to the nucleation sites of earthquakes, likely being influenced by both lithological (material) and rheological (frictional) boundaries.

Plain Language Summary Large strike-slip earthquakes tend to create a zone of fractured network surrounding the main fault. This zone, referred to as a fault damage zone, becomes highly localized as the fault matures, with a width of few hundred meters. The influence of this fault damage zone on earthquake characteristics remains elusive since we do not have enough long-term observations along a single fault. We use numerical simulations to examine the behavior of earthquake nucleation and rupture dynamics on a fault surrounded by a damage zone over a thousand-year timescale. Our simulations reveal that the reflection of seismic waves from the fault damage zone boundaries leads to complexity in earthquake sequences, such as variability in earthquake locations and sizes. We also show that a shallowfault damage zone produces shallower earthquakes with the earthquake depths centered around two locations (bimodal), as opposed to a deep fault damage zone with the earthquake depths centered around a single location (unimodal). Our study suggests that imaging the geometry and physical properties of fault damage zones could potentially give us clues about depths of future earthquakes and improve earthquake probabilistic hazard assessment.

1. Introduction

Natural faults are often approximated as a single plane of intense deformation, macroscopically seen as a principal slip surface. However, geological (e.g., Chester & Logan, 1986; Chester et al., 1993; Lockner et al., 2011), geophysical (e.g., Lewis & Ben-Zion, 2010; Li & Leary, 1990; Unsworth et al., 1997), and geodetic (e.g., Fialko et al., 2002) observations delineate faults as a geometrically complex network of multiple slip surfaces and fractures, with a nested hierarchy of increasing deformation toward the principal slip surface (Figure 1). These damaged rocks exhibit a dense network of fractures, which can be macroscopically approximated as an elastic zone with reduced shear modulus and seismic velocities (Chester et al., 1993; Harris & Day, 1997). Elastic deformation models have explored the effect of fault damage zones in two dimensions on coseismic

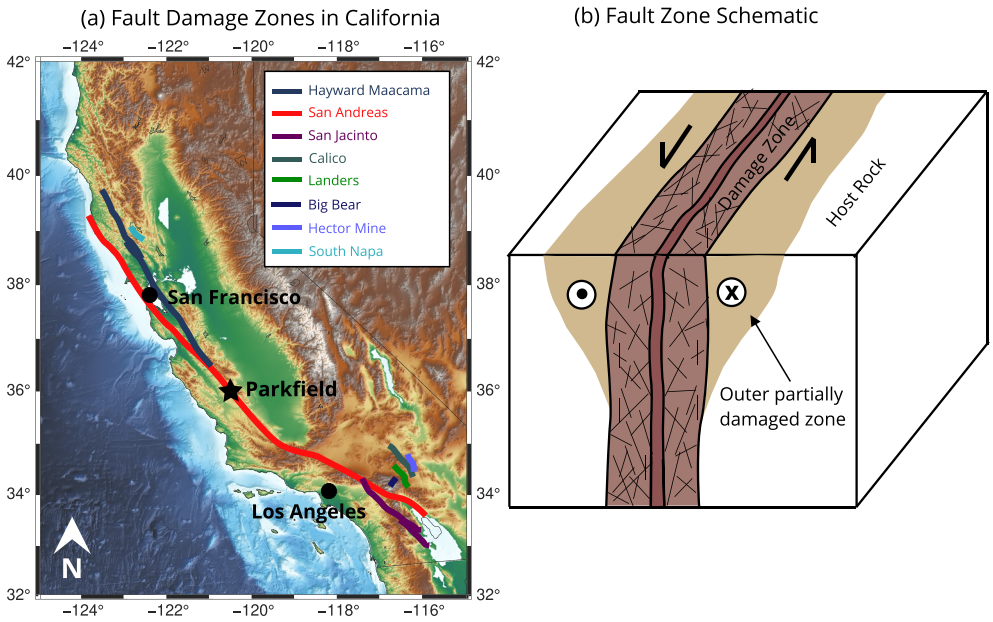

Figure 1. (a) Map of California faults with documented fault damage zones. (b) A schematic of mature fault zone structure that includes a fault core shown as the central dark brown zone surrounded by an inner narrow zone of damage extending through the seismogenic zone, and an outer partially-damaged zone resembling a flower structure (Faulkner et al., 2003; Mitchell & Faulkner, 2009). Our models represent a two-dimensional vertical cross section across the fault.

slip (Barbot et al., 2008), three-dimensional crustal deformation (Barbot et al., 2009), and on patterns of interseismic strain accumulation (Lindsey et al., 2014). The damage zones may exhibit sharp contrast in seismic velocities with respect to the host rock, being capable of trapping seismic waves within the fault zone. The fault damage zone can potentially promote complex stress distribution along faults due to its pronounced dynamic effect on earthquake rupture nucleation and propagation (e.g., Albertini & Kammer, 2017; Harris & Day, 1997; Huang, 2018; Huang & Ampuero, 2011; Huang et al., 2014; Ma & Elbanna, 2015; Weng et al., 2016). We aim to understand the effects of low-velocity damage zones on dynamic rupture propagation and sequence of earthquakes, which include interseismic slip, earthquake nucleation, rupture propagation, and postseismic slip, and study its influence on the variability in earthquake sizes, recurrence intervals, and stressing history of the fault.

Previous numerical models in homogeneous medium (Rundle, 1989; Rundle & Jackson, 1977) and experiments (Mogi, 1962; Scholz, 1968) showed that both mechanical properties of fault rocks and fault stresses can greatly contribute to the variability in earthquake magnitudes and the power law behavior of the magnitude-frequency distribution. Dynamic models of multiple spring-block sliders (Carlson & Langer, 1989; Shaw, 1995) and discrete models of fault slip (Olami et al., 1992) have been successful in reproducing the Gutenberg-Richter distribution and nonuniform recurrence times. Quasi-dynamic continuum models in homogeneous medium have previously used extreme frictional parameters to reproduce observed complexity of earthquakes (Cochard & Madariaga, 1996; Hillers et al., 2006). Recently, Barbot (2019b) and Cattania (2019) have shown that many complexities of fault dynamics, including Gutenberg-Richter distribution of earthquake sizes, can be modeled under quasi-dynamic approximation if the ratio of the fault dimension to the earthquake nucleation dimension is large enough. These models do not assume any structural or material heterogeneities, thus implying that such complexities are a sole manifestation of fault friction. Erickson and Dunham (2014) incorporated a heterogeneous medium in quasi-dynamic earthquake cycle simulations in the form of a sedimentary basin and showed the emergence of subsurface events in addition to surface breaking events. Abdelmeguid et al. (2019) have shown the generation of subsurface events and multiperiod sequences in a low-velocity layered fault damage zone under the quasi-dynamic approximation. Thomas et al. (2014) showed that incorporating inertia in earthquake cycle simulations, that is, fully dynamic simulations, can exhibit significant differences from the quasi-dynamic approximation,

especially under enhanced dynamic weakening frictional behavior. Here we consider fully dynamic models with fault damage zone surrounding mature strike-slip faults. Using fully dynamic earthquake cycle simulations, Kaneko et al. (2011) showed that a fault-parallel, narrow damage zone causes a reduction in the nucleation size of the earthquakes and amplification of slip rates during dynamic earthquake events. Despite a multitude of studies documenting the effects of fault damage zones on single rupture (Harris & Day, 1997; Huang & Ampuero, 2011; Huang et al., 2014), their long-term effects on earthquake sequences are not well understood, partially owing to a lack of seismological records over centuries.

We model earthquake sequences with full inertial effects on a two-dimensional vertical strike-slip fault surrounded by a fault damage zone. The constitutive response of the fault is governed by laboratory-derived rate-and-state friction laws (Dieterich, 1979; Ruina, 1983). This fully dynamic modeling approach can simulate interseismic slip, earthquake nucleation, rupture propagation, and postseismic deformation during multiple seismic cycles in a single computational framework (e.g., Barbot et al., 2012; Jiang & Lapusta, 2016; Kaneko et al., 2011; Lapusta et al., 2000). The fault damage zone is modeled as an elastic layer with a lower seismic wave velocities compared to the surrounding host rock. Other important features of fault damage zones such as off-fault damage generation during the rupture (Ma & Elbanna, 2015; Okubo et al., 2019) and plastic deformation (Huang et al., 2014) have been modeled previously for single earthquake ruptures. We investigate how the wave reflections from fault damage zone modeled as a low-velocity layer influences the long-term stress evolution and contribute to the variability in earthquake magnitudes and hypocenter locations. We show that the variability in earthquake hypocenter is significant only in the cases where the damage zone truncates close to the nucleation site or extends beyond the nucleation zone, suggesting that frictional and rheological effects may be a dominant mechanism for hypocenter variability when the damaged structure is very shallow. Our results also provide a possible explanation for the bimodal depth distribution of seismicity observed along mature strike-slip faults with shallow fault damage zone structures. We describe the observed geometry and material properties of the fault damage zone along the San Andreas Fault that inspire the design of our simulations in section 2. The two-dimensional model setup, model assumptions, friction laws, and simulation methodology are presented in section 3. We demonstrate the effects of the fault damage zone with varying widths and rigidity contrasts on the variability of earthquake magnitudes and hypocenters in section 4.

2. Observed Dimension and Material Properties of Fault Damage Zones

Fault damage zones can be delineated using potential field methods and seismic observations based on trapped waves within the damaged zone. Seismic reflections, magnetotelluric and resistivity surveys along the Parkfield segment of San Andreas Fault reveal a 500 m wide and 4 km deep fault damage zone (Unsworth et al., 1997). This study also suggests a presence of a deeper fault zone whose properties are not well resolved, and a shallow 5 km wider damage zone surrounding the ~500 m wide damage zone, representing a flower structure. Other studies along San Jacinto Fault Zone and San Andreas Fault Zone (e.g., Li & Vernon, 2001; Wu et al., 2010) also indicate that the low-velocity zone may extend to seismogenic depths. Cochran et al. (2009) have combined seismology and geodesy to infer a wide and deep damage zone along Calico fault in Southern California. Fault zone trapped wave studies along the Parkfield segment (Lewis & Ben-Zion, 2010) indicate a 3 to 5 km deep, 150 to 300 m wide fault damage zone, with a potentially nested fault zone extending up to 7 to 10 km. Geologic interpretations on the same region from the SAFOD cores (Lockner et al., 2011) delineate an ~200 m wide fault damage zone at 2.7 km depth. A detailed 3-D seismic wave velocity map (Thurber et al., 2003) also reveals a several hundred meters wide fault zone structure at about 5 to 8 km depth. The shear wave velocity contrast between the host rock and the fault damage zone is found to be around 10% to 60% (Table 1 in Huang et al., 2014, and references therein). Most of these studies report variations in fault damage zone structure along fault strike. We summarize the observed damage zone geometry along the Parkfield segment in Table 1. Fault damage zones have been observed in other regions as well, including the North Anatolian fault in Turkey, the Nojima fault in Japan, and the Kunlun fault in Tibetan Plateau (Ben-Zion et al., 2003; Bhat et al., 2007; Lockner et al., 2000). Based on this short review, it is clear that the fault damage zone width spans several hundred meters, whereas the depth extent is more debatable since the narrow damage zone is more difficult to resolve at depth. We use these observations to guide our model setup as described in the following section.

Table 1
Geometry of Fault Damage Zone Along Parkfield Segment of San Andreas Fault as Constrained by Different Studies

References	Geometry	Width inference	Depth inference
Resistivity and MT (Unsworth et al., 1997)	Wide at the top, narrow at depth	500 m for inner damage, 5 km for outer damage	4 km, with a deeper damage zone less resolved
Trapped seismic waves (Lewis & Ben-Zion, 2010)	Tabular low-velocity zone	150 to 300 m	5 to 7 km
Seismic wave velocities (Thurber et al., 2003)	Wide at the top and at seismogenic depth, narrow in between	500 to 600 m	8 km
Geology: SAFOD (Lockner et al., 2011)	Tabular	200 m	2 km

3. Methodology

3.1. Model Description

We consider a two-dimensional strike-slip fault embedded in an elastic medium with Mode III rupture (Figure 2). This implies that the fault motion is out of the plane and only the depth variations of parameters are considered. The top boundary is stress-free and represents Earth's free surface. The other three boundaries are absorbing boundaries that allow the waves to pass through. Since our model is symmetric across fault, we restrict the computational domain to only one side of the fault. Our domain extends to 48 km depth, where the top 24 km of the fault is bordered at the bottom by a region constantly slipping at 35 mm yr^{11}. This represents the tectonic plate motion that loads the fault and accumulates stresses. The seismogenic zone extends from 2 to 15 km, which is locked during the interseismic period and capable of hosting earthquakes. The rest of the fault creeps aseismically. Earthquakes are captured in our simulations when the maximum slip velocity on the fault exceeds the threshold of 0.001 m s^{-1}. This model is inspired by the San Andreas fault and is similar in setup to Lapusta et al. (2000) and Kaneko et al. (2011).

We model the fault damage zone as an elastic layer with lower seismic wave velocities compared to the host rock. We will focus on how the geometry, spatial extent, and damage intensity of this fault damage zone influence the earthquake sequence behavior. We consider four different scenarios: (I) a homogeneous elastic medium as a reference model, (II, III) a medium with a sharp, narrow fault damage zone with various depths, widths, and velocity contrasts that extends throughout the seismogenic depth in Model II and truncates at a shallow depth in Model III, and (IV) a flower structure in which a narrow fault damage zone

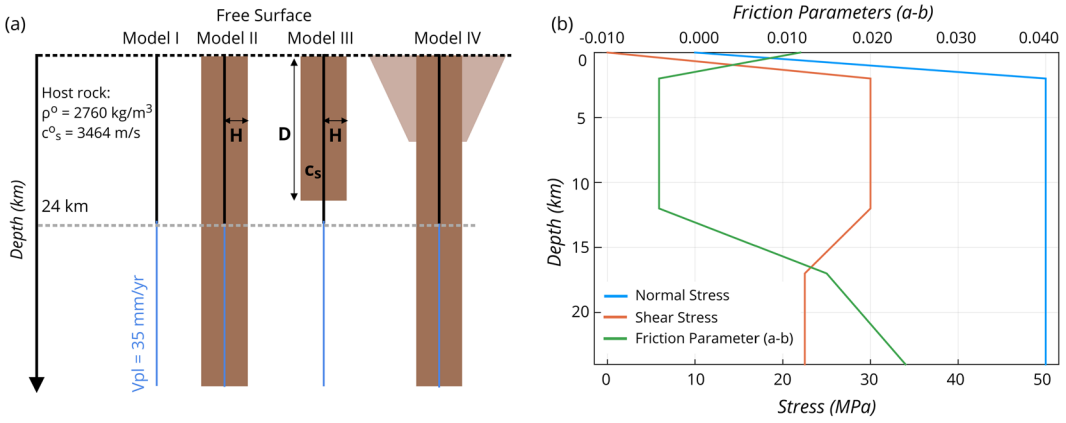

Figure 2. (a) Model description of four different scenarios. We consider a vertical strike-slip fault 24 km deep loaded from below by a plate motion rate of 35 mm yr^{-1}. Model I: Homogeneous medium used as a reference model. Model II: A narrow fault damage zone extending throughout the seismogenic zone. Model III: A narrow fault damage zone truncating at a shallower depth. Model IV: Two-dimensional approximation of flower structure damage. (b) Friction parameters ($a - b$) and initial stresses along the fault dip. The seismogenic zone, that is, the velocity weakening region, is the overstressed patch between 2 and 15 km depth.

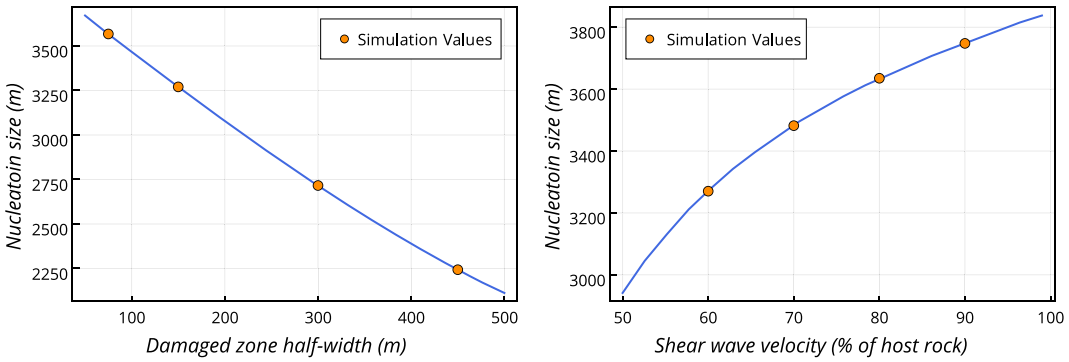

Figure 3. Variation of theoretical nucleation sizes in a layered medium. The left figure shows the variation due to fault damage zone widths, and the right figure shows the variation due to shear wave velocity. The orange dots show the theoretical nucleation sizes for the parameters chosen in our simulations.

extending through the domain surrounded by a wider, trapezium-shaped fault damage zone truncated at a shallow depth (Figure 2). In natural settings, the outer trapezium-shaped fault damage zone may not have a sharp boundary at depth but may show a smooth transition because its structure is more diffused than the inner fault damage zone. We use a sharp boundary at a depth of 8 km as an approximation of the flower structure in order to highlight the effects of dynamic wave reflections. These four sets of models are described in Figure 2. We vary the width (H) and shear wave velocity (c_s) contrast of the fault damage zone in the Model (II) and the depth (D) in Model III to study their effects on earthquake sizes and hypocenters (Figure 2a). The choices of H and c_s are shown in Figure 3. We choose four different values of D including two depths (6 and 8 km) shallower than the nucleation site in the homogeneous medium, one depth intersecting the nucleation zone (10 km) and one depth extending beyond the nucleation zone (12 km). In the model (IV), the outer, wider fault damage zone has a shear wave velocity reduction of 20% compared to the host rock, while the inner one has a 40% reduction. The second and third models are inspired by the geological and geophysical observations of the San Andreas fault zone as discussed in section 2, and the fourth model is inspired by the classic flower structure of fault damage zones (Caine et al., 1996; Pelties et al., 2015; Perrin et al., 2016; Sibson, 1977; Unsworth et al., 1997).

3.2. Friction Laws

The laboratory-derived rate- and state-dependent friction laws relate the shear strength on the fault to the fault slip rate (Dieterich, 1979; Ruina, 1983; Scholz, 1998). We use the regularized form for the shear strength interpreted as a thermally activated creep model (Lapusta et al., 2000; Rice & Ben-Zion, 1996), which relates the shear strength (T) to the slip rate ($\dot{\delta}$) as follows:

$$T = a\sigma \operatorname{arcsinh}\left[\frac{\dot{\delta}}{2\dot{\delta_o}} e^{\frac{f_o + b\ln(\dot{\delta}\theta/L)}{a}}\right] \tag{1}$$

where σ is the effective normal stress (the difference between lithostatic stress and the pore fluid pressure), f_o is a reference friction coefficient corresponding to a reference slip rate $\dot{\delta_o}$, and a and b are empirical constants dependent on the mechanical and thermal properties of the contact surface. The parameter θ is a state variable interpreted as the average lifetime of the contact asperity, and L is the characteristic distance over which most of the evolution in shear resistance occurs, as measured in the laboratory during velocity steps. Barbot (2019a) has also shown that the state variable θ is the age of contact strengthening. In our models, the evolution of the state variable is governed by the aging law:

$$\frac{d\theta}{dt} = 1 - \frac{\dot{\delta}\theta}{L} \tag{2}$$

The frictional stability of faults is determined by the frictional parameters, L, $(a-b)$, and the ratio $\frac{a}{b}$. Depending on the value of $(a-b)$, we can have an unstable slip for a steady state velocity weakening

frictional regime $(a-b)<0$, or a stable sliding for a steady state velocity-strengthening frictional regime $(a-b)>0$. Earthquakes occur when the velocity-weakening region of the fault exceeds a critical nucleation size that depends on the shear moduli of near-fault rocks, effective normal stress and frictional parameters (Rice, 1993; Rubin & Ampuero, 2005). More generally, the fault dynamics is controlled by R_u, the ratio of the velocity-weakening patch size to the nucleation size, and the ratio $\frac{b-a}{a}$ that controls the relative importance of strengthening and weakening effects and the ratio of static to dynamic stress drops. For higher values of R_u, we can obtain more chaotic rupture styles such as partial and full ruptures, aftershock sequence, and a wide range of events. For our simulations, the theoretical nucleation size is ∼2 km, and the width of velocity weakening region is ∼10 km, implying the value of $R_u \sim 5$, which predicts single-period full ruptures (Barbot, 2019b).

We use a depth dependent profile for $(a-b)$ as inferred from granite samples in laboratory experiments (Blanpied et al., 1991, 1995). The seismogenic zone is the velocity weakening region extending from a depth of 2 to 15 km. The rest of the fault is velocity strengthening and accommodates aseismic creep. The velocity-strengthening region at the top 2 km of the fault is suggested by laboratory observations under low stresses (Blanpied et al., 1991). The effective normal stress is assumed constant below the depth of 2 km, since the increase in the lithostatic stress is accommodated by the pore fluid pressure at depth (Rice, 1993). The seismogenic zone is overstressed initially (Figure 2b). Blanpied et al. (1991) also shows the temperature weakening behavior of the friction for higher temperatures, but we only use the velocity dependence of the friction in this study. Barbot (2019a) derived an alternative formulation that incorporates thermal dependence of fault strength and provides an explicit relationship between frictional parameters and micromechanical properties. We have chosen a relatively standard model of the regularized rate- and state-dependent friction described by Rice and Ben-Zion (1996) and Lapusta et al. (2000), so that it is easier to compare the results with previous studies.

3.3. Numerical Simulation of Fully Dynamic Earthquake Sequences

We use a spectral element method to simulate dynamic ruptures and aseismic creep on the fault (Kaneko et al., 2011). Full inertial effects are considered during earthquake rupture and an adaptive time stepping technique is used to switch from interseismic to seismic events based on a threshold maximum slip velocity of 0.5 mm s^{-1} on the fault. This method is able to capture all four phases of the earthquake cycle including nucleation, rupture propagation, postseismic deformation, and interseismic creep. We implement Kaneko et al.'s (2011) algorithm in Julia (Bezanson et al., 2017) using a more efficient linear solver based on the Algebraic Multigrid scheme (Ruge & Stüben, 1987) for the elliptic (interseismic) part of the earthquake sequence. We use the Algebraic Multigrid as a preconditioner while solving the sparse linear system using the conjugate gradient method. This combines the superior convergence properties of the Algebraic Multigrid with the stability of Krylov methods and is very well suited for symmetric, positive definite matrices. This iterative technique uses a fixed number of iterations independent of the mesh size. Landry and Barbot (2016, 2019) have derived the equations to solve elliptic equations using the Geometric Multigrid in 2-D and 3-D. While the Geometric Multigrid has superior convergence properties, the Algebraic Multigrid is better suited for more complicated meshes and is scalable to a wide variety of problems as the solver works with the numerical coefficients of the linear system as opposed to the mesh structure. The detailed algorithm is described in Tatebe (1993). In addition, we use the built-in multithreading feature of Julia, which enables us to achieve a CPU speed-up of ∼50 times compared to the original code described in Kaneko et al. (2011).

3.4. Theoretical Nucleation Estimates and Choice of L

In a two-dimensional continuum model, the theoretical estimate of earthquake nucleation for a Mode III crack based on energy balance is given by (Rubin & Ampuero, 2005)

$$h^* = \frac{2}{\pi}\frac{\mu L b}{\sigma(b-a)^2} \tag{3}$$

where a,b, and L are the rate and state friction parameters, μ is the shear modulus of the near-source region, and σ is the effective normal stress. We note that the above estimate of nucleation size is not a unique estimate but is appropriate for our choice of friction parameters (Kaneko & Lapusta, 2008;

Rubin & Ampuero, 2005). Using $L = 8$ mm leads to a nucleation size of 3.9 km in a homogeneous medium. As the nucleation size is proportional to the rigidity of the near-source medium (Kaneko et al., 2011; Rubin & Ampuero, 2005), it is reduced by a factor of ~3 in a damaged medium with a shear wave velocity reduction of 40% (Huang, 2018). The theoretical estimate of the nucleation size in a layered medium (h^*_{lay}) for a Mode III rupture is derived by Kaneko et al. (2011) using linear stability analysis:

$$h^*_{lay}\tanh\left[2H\frac{\gamma}{h^*_{lay}} + \operatorname{arctanh}\left(\frac{\mu_D}{\mu}\right)\right] = h^*_{hom} \tag{4}$$

where μ and μ_D are the rigidity of the host rock and the layer respectively, γ ($= \pi/4$) is an empirical parameter dependent on the geometry, h^*_{hom} is the theoretical nucleation size in the homogeneous medium with reduced shear modulus, and H is the thickness of the layered medium. The parameter choice of width and shear wave velocity contrast and their corresponding nucleation sizes are shown in Figure 3. A smaller nucleation size would allow smaller earthquakes to nucleate successfully, therefore incorporating a wider range of magnitudes. We use five Gauss-Lobatto-Legendre nodes inside each spectral element, such that the average node spacing is 20 m. For a well resolved simulation, the cohesive zone size (Day et al., 2005; Kaneko et al., 2008) should contain at least three node points. Based on the frictional parameters and rigidity of fault damage zone, the quasi-static cohesive zone size in our models is ~120 m and encompasses sufficient nodes. We demonstrate the convergence of our model with respect to different node spacings in Appendix A.

4. Results

4.1. Complexity in Fault-Slip Due to Damage Zone

We discuss the slip-complexity due to reduction in nucleation size in a homogeneous medium and subsequently due to a fault damage zone as a layered medium. The theoretical nucleation size of a Mode III rupture is directly proportional to the rigidity of the medium. Since smaller nucleation sizes also tend to give rise to complexities in earthquake cycles (Lapusta & Rice, 2003), it is imperative to isolate the effects of reduced nucleation size from the effects of dynamic wave reflections and stress heterogeneities due to fault damage zones. In this section, we analyze three simulations, all having comparable nucleation sizes: (a) A homogeneous medium simulation with a reduced characteristic slip distance (Figure 4a), (b) a homogeneous medium simulation with a reduced shear modulus, that is, the entire medium is damaged (Figure 4b), and (c) a simulation with a fault damage zone modeled as a narrow low-velocity layer (Figures 4c–4e). The simulation parameters for each of these models are discussed in Table 2. We see that Figures 4a and 4b host earthquakes with uniform sizes and hypocenter locations. We also observe an increase in recurrence intervals and accumulated slip in Figure 4b compared to Figure 4a, which can be attributed to a reduced shear modulus in the medium. Despite these differences, we do not observe complexities such as variations in hypocenter locations or earthquake sizes. In contrast, Figures 4c–4e show significant variability in both earthquake size and hypocenter location, which is attributed to dynamic wave reflections. The damaged medium also has a much larger coseismic slip when compared to an undamaged medium. Figure 4f shows the comparison of slip rate and shear stress evolution at 7 km for the three representative models (Figures 4a–4c), demonstrating the effect of dynamic wave reflections on stress heterogeneities. We see a clear reflection phase from the free surface in all the models, but the slip rate and the shear stress is much more heterogeneous in our fault damage zone model. The dynamic wave reflections generate peaks in the shear stress profile that persist through multiple earthquake sequences. It is clear from this comparison that inertial dynamics play an important role in the earthquake sequences, especially in layered medium such as our fault damage zone models.

Our results show that the presence of the fault damage zone promotes complexity in the earthquake slip distribution and variability in their magnitudes, especially for large rigidity contrast between the fault damage zone and the host rock. Given the friction parameters and initial stress conditions in our simulations (Table 2), the homogeneous medium hosts periodic earthquakes with exactly the same hypocenter locations and magnitudes, whereas the fault surrounded by a fault damage zone shows a more complex slip distribution with variable earthquake sizes and hypocenter locations through multiple earthquake cycles

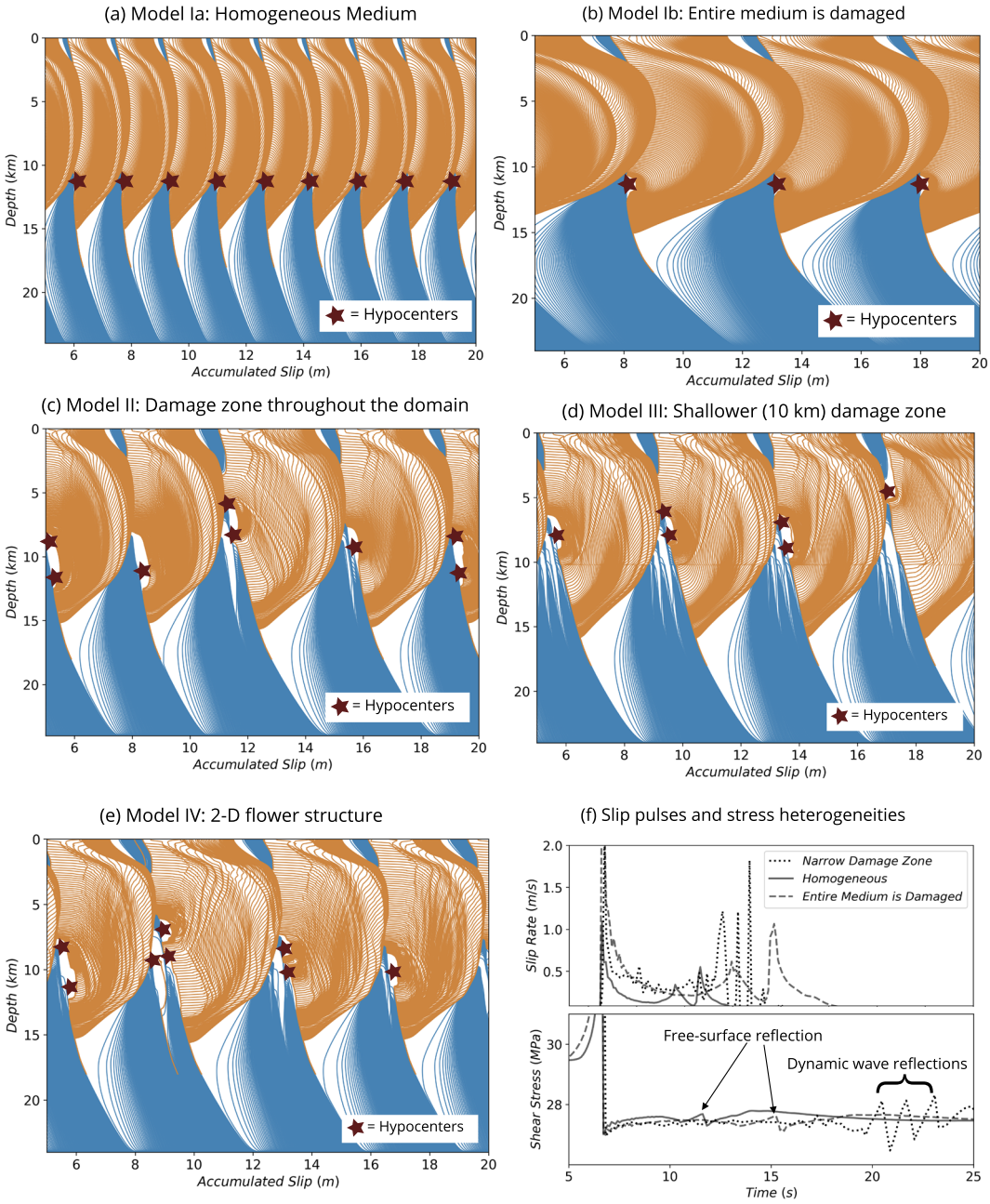

Figure 4. Cumulative slip contours with hypocenters shown as red stars. Multiple hypocenters close to each other represent smaller (Mw ~3) and larger (Mw ~7) earthquakes. The orange lines are plotted every 0.1 s during an earthquake and the blue lines are plotted every 2 yr during the interseismic period. The different models include (a) Homogeneous medium with smaller $L = 4$ mm, (b) homogeneous medium with reduced shear modulus $\mu = 10$ GPa such that the entire medium is damaged, (c) a narrow fault damage zone extending throughout the fault, (d) a narrow fault zone truncated at shallow depth, and (e) 2-D flower structure. (f) Comparison of slip rate and shear stress for a single rupture of three models shown in Figures 4a–4c.

(Figures 4c–4e). We use comparable nucleation sizes for the homogeneous medium and damaged models to highlight the effects of dynamic waves. We also observe ruptures with multiple slip pulses and more complex slip distribution in the flower structure scenario (Figures 4e and 5b).

Previous dynamic rupture simulations show that fault zone wave reflections can induce pulse-like ruptures (Harris & Day, 1997; Huang & Ampuero, 2011; Huang et al., 2014). We observe the imprint of these wave reflections in the spatiotemporal slip rate evolution of fault damage zone simulations (Figure 5). These

Table 2
Parameters Used in Numerical Simulations of Earthquake Cycles

Parameter	Symbol	Value
Static friction coefficient	μ_0	0.6
Reference velocity	V_0	1×10^{-6} m s^{-1}
Plate loading rate	V_{pl}	35 mm yr^{-1}
Evolution effect	b	0.019
Effective normal stress	σ	50 MPa
Initial shear stress	τ_0	30 MPa
Steady-state velocity dependence in the seismogenic region	$(b-a)$	−0.004
Width of seismogenic zone	W	10 km
Average node spacing	dx	20 m
Seismic slip rate threshold	V_{th}	1 mm s^{-1}
	Model Ia: Undamaged medium	
Characteristic weakening distance	L_c	4 mm
Shear modulus	μ	32 GPa
	Model Ib: Entire medium is damaged	
Characteristic weakening distance	L_c	8 mm
Shear modulus	μ	16 GPa
	Model II and III: Layered medium	
Characteristic weakening distance	L_c	8 mm
Shear modulus of host rock	μ	32 GPa
Shear modulus of damaged rock	μ_D	10 GPa
Model IV: 2-D flower structure		
Characteristic weakening distance	L_c	8 mm
Shear modulus of host rock	μ	32 GPa
Shear modulus of inner damage zone	μ_{Di}	18 GPa shear modulus
of outer damage zone	μ_{Do}	10 GPa

Note. The parameters shown at the beginning are the same for all the simulations and other parameters are shown for each model that we use. The normal and shear stresses represent the values for the velocity-weakening region.

slip pulses become a dominant feature during earthquake rupture as the waves are reflected from the damage zone boundaries in our earthquake cycle simulations. Similar pulse-like ruptures are also observed inhomogeneous medium earthquake cycle simulations for specific sets of heterogeneous friction parameters and fault asperity dimensions (Michel et al., 2017). Our results suggest that stress heterogeneities generated by slip pulses due to seismic wave reflections are primarily responsible for the complexities in accumulated slip and variation in hypocenter distributions.

We compute the moment magnitudes of simulated earthquakes to investigate the relation between the magnitudes and cumulative number of earthquakes. The start and end of a rupture is defined based on a threshold slip velocity of 0.001 m s^{-1}. The seismic moment is calculated as the product of the elastic shear modulus (μ), the coseismic slip (D) integrated along the depth, and the rupture area. The rupture length (L) is defined as the part of the fault where slip is greater than 1% of the maximum coseismic slip during a certain earthquake. Since our simulation is two-dimensional, we assume the rupture width (W) is the same as the rupture length. The seismic moment (M_o) is defined as

$$M_o = \mu(LW)D = \int dL \int \mu(dL)D(L) \tag{5}$$

The moment magnitude is computed using the relation of Kanamori and Anderson (1975): $Mw = 2/3\log_{10} M_o - 10.7$, where M_o is the seismic moment measured in dyne centimeters.

In our simulations, the model with homogeneous medium hosts one large earthquake every ~100 yr. The recurrence intervals and magnitude of the earthquakes are also fairly uniform throughout the seismic cycle. In the presence of the fault damage zone, we observe more complex slip history with varying earthquake magnitudes and hypocenter locations. To further understand the simulated earthquake catalog, we investigate the number of earthquakes for each magnitude range (i.e., magnitude-frequency distribution). We combine the magnitudes for all the fault zone simulations in order to emulate a natural setting where there are

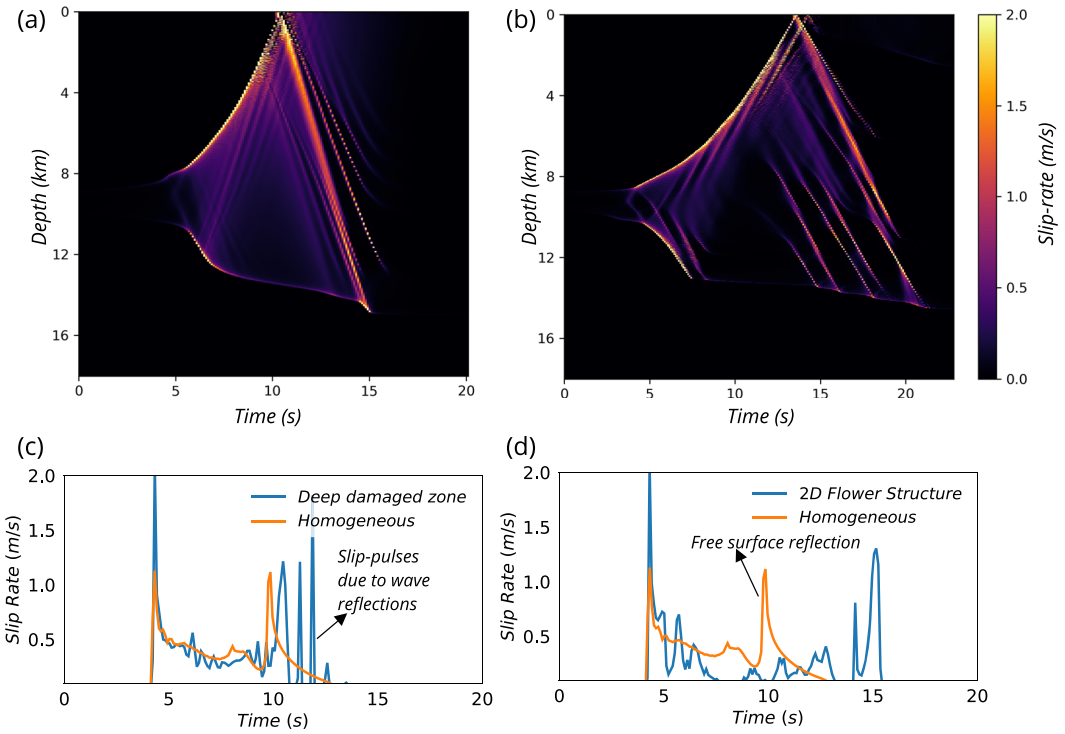

Figure 5. Spatiotemporal slip rate evolution demonstrating dynamic wave reflections for (a) fault damage zone extending throughout the domain, and (b) trapezoid-shaped nested fault damage zone. (c and d) The slip rate at a depth of 7 km for (a) and (b), respectively, as compared to a homogeneous medium. The ruptures begin as crack but transition to pulses due to the wave reflections.

multiple faults with varying fault damage zone properties and show their cumulative magnitude-frequency distribution in Figure 6a. We observe a decrease in the number of earthquakes as the magnitude increases from 3 to 4.5, after which the number of earthquakes stagnates for intermediate magnitudes of 4.5 to 6. Finally, we see a sharp decrease in the number of earthquakes for the largest earthquakes. This combined magnitude-frequency distribution is different from the Gutenberg-Richter distribution.

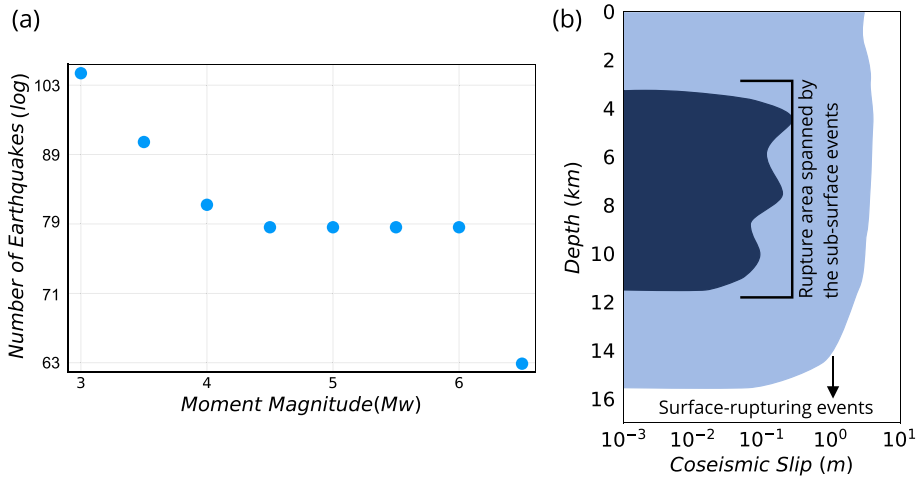

Figure 6. (a) Cumulative magnitude-frequency distribution for the combined simulations with multiple fault damage zone widths, depths, and rigidity contrasts. (b) The envelope of coseismic slip for the larger and smaller earthquakes against are plotted against the fault depth. We show the cumulative rupture length (and therefore rupture area) for all the larger and smaller earthquakes combined as the shaded region.

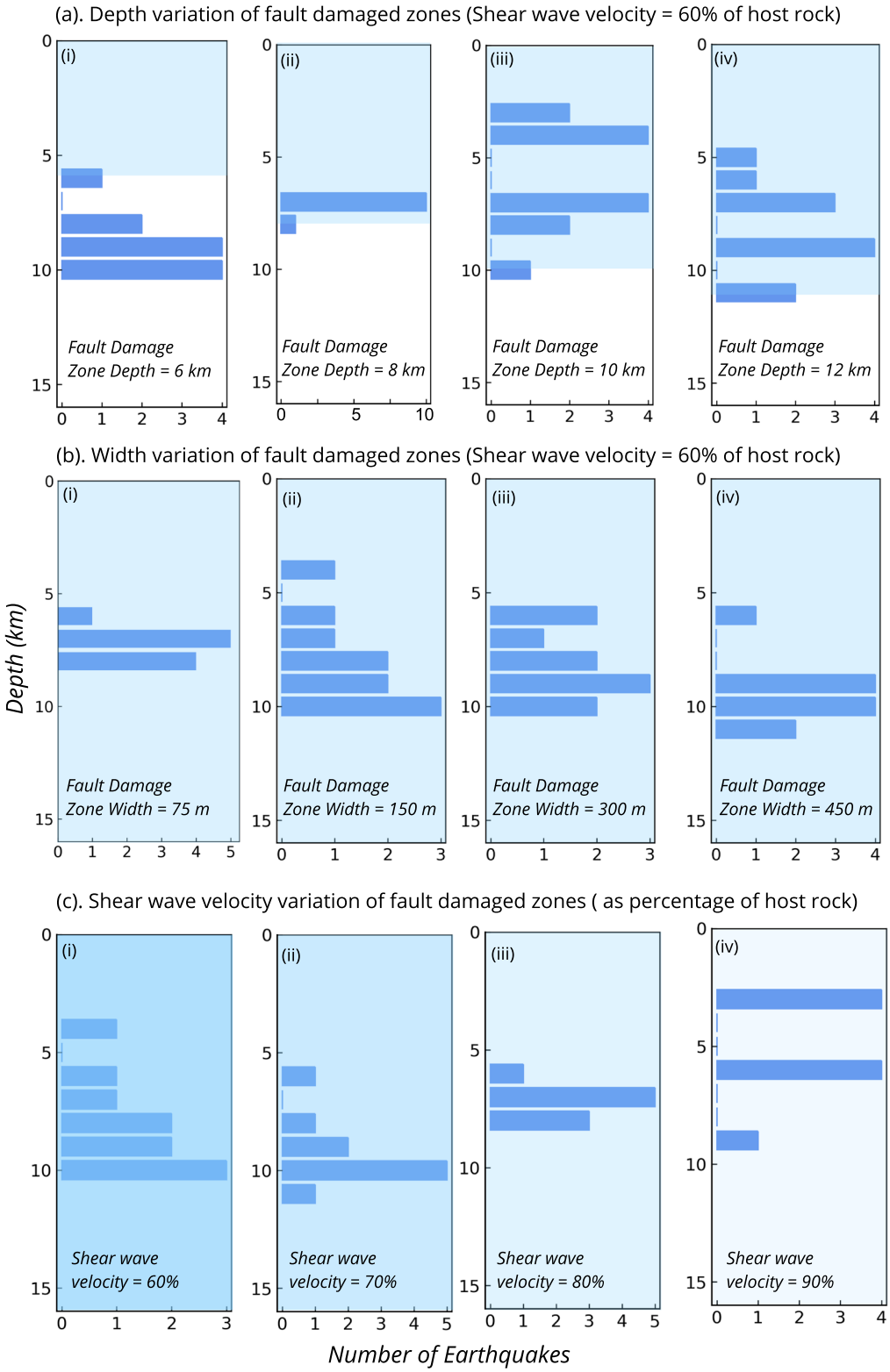

Figure 7. Earthquake hypocenter distribution for simulations with varying (a) fault damage zone depths, (b) widths, and (c) shear wave velocity contrasts. The shaded region shows the depth extent of damage zone and the intensity of shading shows the shear wave velocity contrast. All the models are shown to a depth of 16 km, which is the transition from velocity-weakening to velocity-strengthening regime.

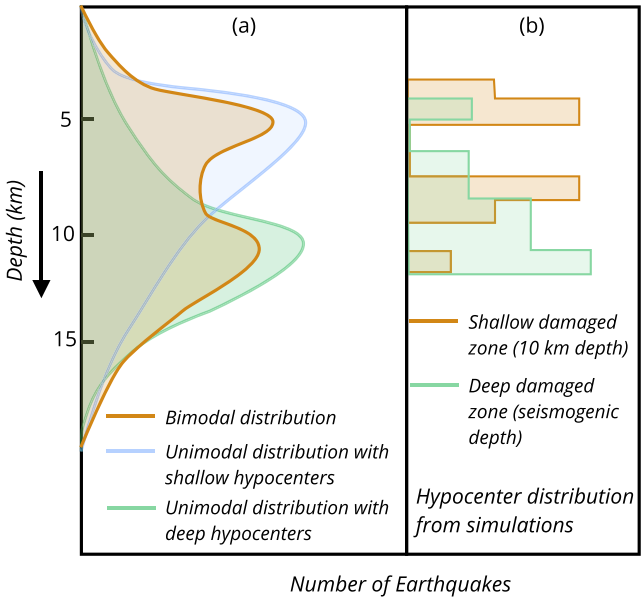

Figure 8. (a). Observed seismicity distribution along strike-slip faults. We show bimodal distribution (Hauksson & Meier, 2019; Mai et al., 2005; Marone & Scholz, 1988), unimodal distribution with shallow hypocenters (Kim et al., 2016; Powers & Jordan, 2010), and unimodal distribution with deep hypocenters (Hauksson & Meier, 2019). (b) Simulated hypocenter distribution for a shallow and a deep damage zone. The models correspond to Figures 7a (iii) and 7b (ii).

To understand the gap in the intermediate magnitude earthquakes, we examine the envelope of the coseismic slip distributions representing the rupture area for all the simulated earthquakes (Figure 6b). The rupture areas of smaller earthquakes are confined within the depth range of 3 to 11 km (Figure 6b). The rupture area and final slip for these subsurface events are ~10 times smaller than those of the surface-rupturing events. Therefore there is 2 orders of gap in the moment magnitudes between the small and large events. Since the effective normal stress and hence the fault strength is low at depths shallower than 3 km, it is harder to stop dynamic ruptures once they reach this shallow depth. When the rupture breaks through the free surface, the magnitude of the earthquakes tend to be much larger, which may explain the lack of intermediate magnitude earthquakes. Another potential reason is that there is no along-strike rupture termination in our 2-D models. Generating a Guternberg-Richter type earthquake catalogue may require a reduction in earthquake nucleation size (Cattania, 2019), additional frictional or material heterogeneities, or along-strike termination of spontaneous ruptures.

4.2. Variability in Earthquake Hypocenters

Earthquakes on crustal strike-slip faults tend to occur within the top 15 to 20 km of the crust, known as the seismogenic zone. However, these earthquakes are not uniform along depth and are more correlated with the shallow crustal structure (Marone & Scholz, 1988). Mai et al. (2005) have performed Kolmogorov-Smirnov tests on a database of finite-source inversions and showed that the uniformity of hypocenters along depth can be statistically rejected, especially for strike-slip faults. Other studies (Hauksson & Meier, 2019; Marone & Scholz, 1988) have shown that the depth distribution of earthquake hypocenters may be more bimodal, with strong clustering of earthquakes at shallow (~5 km) and deeper (~15 km) depths. A bimodal distribution for rupture sizes has also been observed in thrust fault settings (Dal Zilio et al., 2019). Shallow seismicity is usually interpreted as short-term strain transients or changes in the frictional and rheological properties of rocks along depth. The abrupt decrease in deeper seismicity (≤15 km) is attributed to the thermomechanical behavior of rocks at these depths. We provide an alternate explanation for the bimodal distribution of seismicity along strike-slip faults based on the geometrical extent of fault damage zones, wherein the structural boundary of the fault damage zone produces additional stress concentration that promotes earthquake nucleation near the boundary. Our results also suggest that frictional and rheological effects may be a dominant mechanism for hypocenter variability when the damaged structure is shallower than 8 km.

The depth distributions of earthquake hypocenters for various fault zone depths, widths and velocity contrasts are shown in Figure 7. In contrast to the homogeneous medium, the hypocenter locations vary considerably for the fault zone simulations, and the depth extent of the fault damage zone has a pronounced effect on the hypocenter location. As demonstrated by Figure 7a, the maximum variability in hypocenter locations is observed when the fault damage zone extends to the earthquake nucleation sites. As the fault zone becomes deeper, we see a systematic downward shift in the average hypocenter location, which saturates for a very deep fault zone extending throughout the seismogenic zone. We attribute this variability to the sharp material discontinuity between the fault damage zone and the host rock where shear stress changes tend to be concentrated (Bonafede et al., 2002; Rybicki & Yamashita, 2002), resulting a number of earthquakes nucleating near this interface. For the same depth below the shallower fault zone, the deeper fault zone leads to a smaller nucleation size due to the reduction in elastic shear modulus, thus allowing earthquakes to nucleate at a deeper location as the fault is loaded from below. However, when the damage zone is very shallow, in the order of ~6 km depth (Figures 7a–7i), most of the earthquakes nucleate below the damage zone. This suggests that the interplay between the earthquake nucleation site and damage zone boundary is an important factor influencing earthquake hypocenter locations. Despite additional stress concentration at the fault damage zone boundary, fault loading conditions and frictional boundary have a

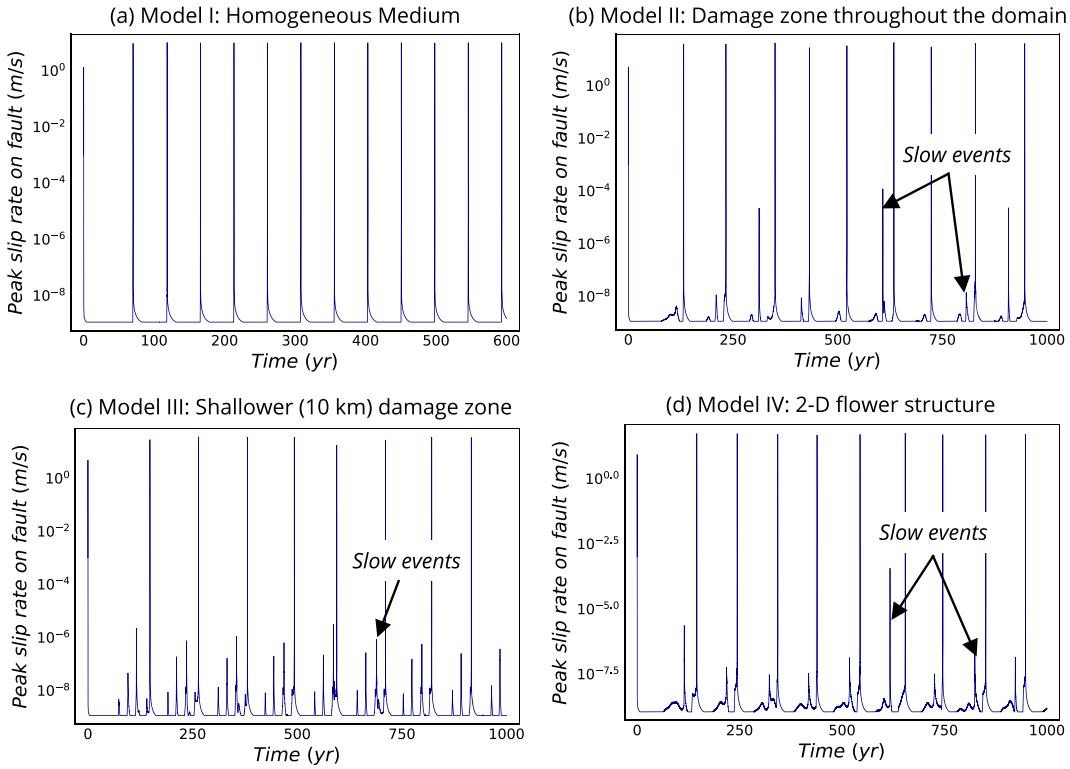

Figure 9. Peak slip rate function for (a) homogeneous medium, (b) deep fault damage zone, (c) shallow fault damage zone, and (d) two-dimensional flower structure.

dominant effect on earthquake hypocenters for very shallow fault zone. But as the fault damage zone penetrates to the nucleation site, the fault zone effects become more critical in determining the depth distribution of seismicity. In other words, the seismicity distribution is influenced by both the material and frictional boundaries.

In fault damage zones extending throughout seismogenic depths, the increase of damage zone width also leads to an increase in the average hypocenter depths (Figure 7b). This is consistent with the idea that the nucleation size is reduced as the width increases, which should lead to a downward shift in earthquake hypocenters when the fault loaded from below. The hypocenter locations also tend to be deeper for a higher shear wave velocity contrast, again due to a smaller nucleation size (Figure 7c).

Our simulations highlight the variable depth distribution of earthquake hypocenters on strike-slip faults. In certain cases, a shallow fault damage zone exhibits more bimodal distribution of hypocenters (Figure 7a, iii), whereas deeper fault damage zones tend to exhibit more unimodal distribution (Figure 7b, ii). We also see a bimodal distribution when the shear wave velocity contrast is very low (Figure 7c, iv), which can be attributed to frictional stress concentrations. We show the hypocenter distributions from two representative simulations of a shallow and a deep fault damage zone against various observations (Figure 8a), wherein the shallower damage zone shows a more bimodal distribution as compared to a deeper damage zone (Figure 8b). It is pertinent to note that most of the observations of seismicity depth distribution is limited to small earthquakes, because we do not have enough record of large earthquakes along single faults. Nevertheless, we are qualitatively able to compare the simulated earthquake hypocenter locations with the observed hypocenter locations.

4.3. Evolution of Peak Slip Rate and Fault Shear Stresses

We show the peak slip rate evolution for our simulations in Figure 9. A homogeneous medium simulation shows large recurring earthquakes, whereas smaller events emerge in a damaged medium, caused by the interplay between the fault damage zone boundary and the nucleation along the fault. In addition, we

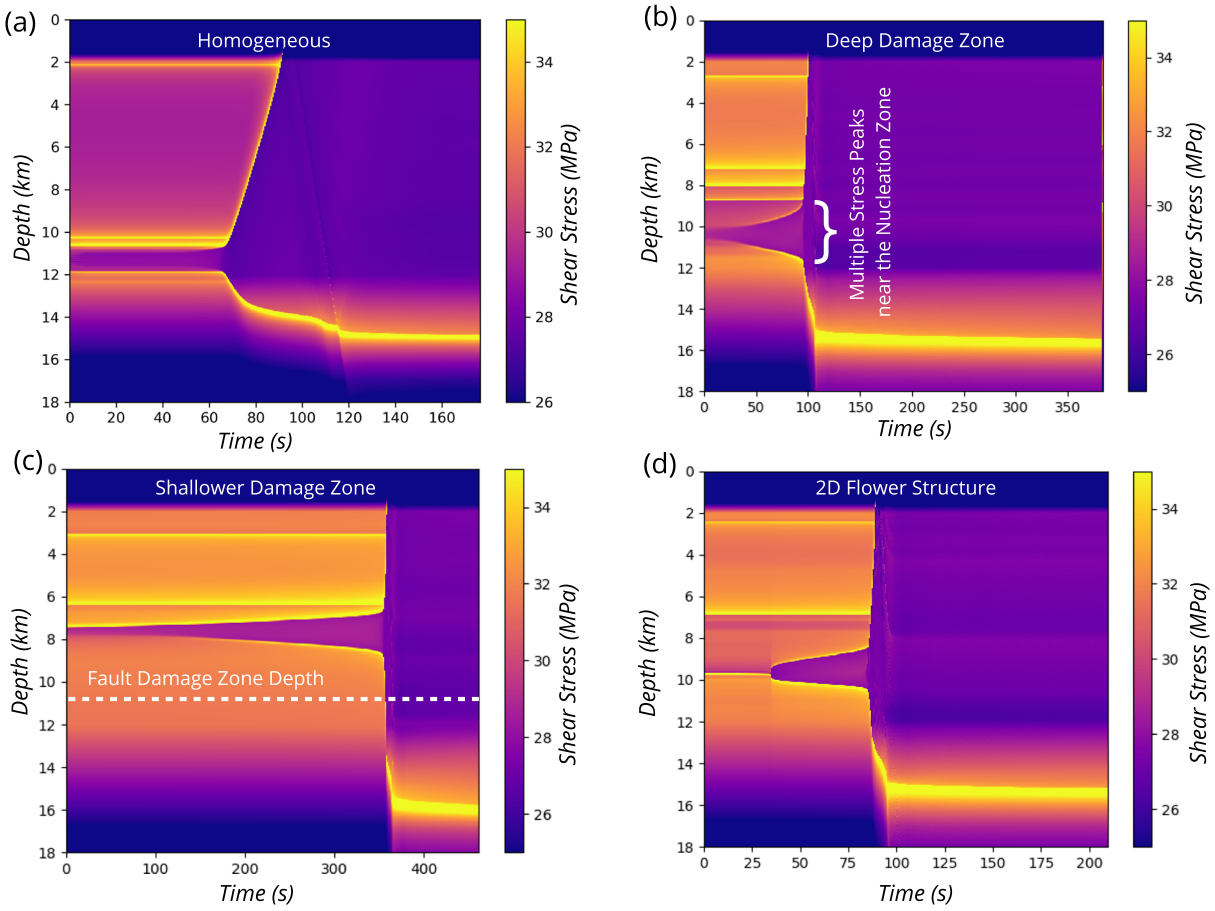

Figure 10. Shear stress evolution of a single earthquake including the nucleation phase shown along the fault for (a) homogeneous medium, (b) deep fault zone, (c) shallower fault zone, and (d) two-dimensional flower structure.

observe multiple slow events in the presence of the fault damage zone that do not grow to fully dynamic earthquakes. The complexities in the number of these slow events are elevated for a shallow fault damage zone extending to the nucleation site (Figure 9c). The flower structure shows a more complex peak slip rate function (Figure 9d) despite having fewer slow events because the inner damage zone extends deep within the seismogenic zone. These slow events in our models occur at ~10 km depth (Figures 4d and 4e), close to the nucleation site and also close to the damage boundary in the case of shallower fault damage zone (Figure 4d). They can be interpreted as accelerations in the slip rate that cannot grow to fully dynamic earthquakes because the stresses are not large enough to reach the dynamic regime, that is, a failed nucleation (Barbot, 2019b; Noda & Hori, 2014). We observe a combination of slow events and dynamic ruptures in the velocity weakening regime. Our results imply that the geometry of the damaged medium can cause additional source complexities that are similar to seismic observations. We infer that a mature fault zone is more likely to exhibit slow events compared to immature fault zones in strike-slip tectonic settings.

In order to understand the mechanism underlying the variability of earthquake hypocenter locations and the scale of stress heterogeneities, we show the temporal evolution of fault shear stresses for different types of fault zones. Figure 10 shows the shear stress evolution for the largest earthquake in homogeneous medium, a deeper fault damage zone, a shallow fault damage zone, and the 2-D flower structure, respectively. Ruptures in the fault zone undergo a transition from cracks to pulses predominantly after the waves are reflected from the fault damage zone boundaries (Figure 5a), while the homogeneous medium simulations maintain crack like ruptures. We observe shear stress heterogeneities emerging during the nucleation phase in the damage zone simulations (Figure 10b), whereas they are absent in homogeneous medium

(Figure 10a). The interference of multiple stress peaks very close to the nucleation site are responsible for the variability in earthquake hypocenter locations and sizes in the fault zone simulations. The emergence of smaller earthquakes (Mw ~3.0) and the slow events are prominent when a fault damage zone extends to the nucleation site of the earthquakes. Although earthquake rupture velocities are slower in the fault damage zone, the stress peak amplitudes are larger than the homogeneous medium. Overall, the two key effects of the fault damage zoned in fully dynamic earthquake sequences are (a) multiple stress peaks near the nucleation site and (b) small-scale stress heterogeneities due to dynamic wave reflections.

5. Discussion and Conclusions

We present fully dynamic earthquake cycle models that incorporate near-fault material heterogeneities represented by a fault damage zone. We show that the fault zone waves can lead to earthquakes with variable magnitudes and hypocenter locations. The depth distribution of earthquake hypocenters is strongly affected by the fault damage zone depth, with shallower fault zones favoring shallower hypocenters. We also see a bimodal depth distribution of earthquake hypocenters in shallow damage zones and a more unimodal distribution in deeper damage zones. The variable nucleation locations originate from the interaction between stress heterogeneity induced by dynamic fault zone waves and the rate and state fault. In the shallow fault zone, the stress peaks are concentrated near the bottom of the fault damage zone and directly correlated with the earthquake nucleation locations, whereas the complex nucleation phase is absent in the homogeneous media.

Most existing studies that have discussed complexities in earthquake sequences with a damaged zone use a radiation damping approximation in a quasi-dynamic framework to accommodate the effects of inertia. A major shortcoming in the quasi-dynamic framework is the absence of radiated waves. We have demonstrated that the reflected wave from a fault damage zone can have strong effects on shear stress distribution, and these effects can lead to complexities in the earthquake behavior such as the earthquake size and the hypocenter location. Thomas et al. (2014) have shown a detailed comparison of quasi-dynamic versus fully dynamic earthquake cycle simulations and they demonstrate significant quantitative and some qualitative differences between the two. In particular, the radiation damping approximation tends to show crack-like behavior, whereas pulse-like behavior is easily obtained in fully dynamic simulations. The addition of enhanced dynamic weakening leads to significant changes in the earthquake behavior simulated using fully dynamic simulations. The effects of full inertial dynamics have not been explored on the entire parameter space consisting of different ratios of the velocity-weakening size to the nucleation size due to the huge computation cost associated with simulating these fully dynamic earthquake sequences. Even in homogeneous medium simulations without a fault damage zone, it is not clear if models accounting for full inertial dynamics would lead to the same conclusion as Barbot (2019b) and Cattania (2019). Nevertheless, previous studies such as Thomas et al. (2014) and our current work suggest that major changes are expected, and the quasi-dynamic approximation should be used with caution. In particular, we have demonstrated that for the same nucleation size, the dynamic wave reflections lead to pulse-like behavior and therefore additional complexity in the earthquake sequences.

Previous static and quasi-dynamic simulations have shown that perturbations in shear and normal stress can give rise to complex seismicity (Ben-Zion, 2001; Perfettini et al., 2003). Furthermore, observations and numerical experiments suggest that the tectonic stresses on real faults are spatially heterogeneous (Rivera & Kanamori, 2002; Townend & Zoback, 2000), implying that the stress amplitudes are not smooth but oscillatory over space. The emergence of persistent slip pulses after initial few seconds of rupture propagation contribute to stress heterogeneity in our simulations. Another key observation is the emergence of smaller, slower events in the damaged medium that do not grow to dynamic earthquakes. These slow events are more prominent in the shallow fault zones where the depth of the fault damage zone intersects the nucleation zone but does not extend deeper to the seismogenic zone. This suggests that the material heterogeneities strongly influence the nucleation phase in addition to generating dynamic reflected waves.

We find that the shape and properties of damage zone can affect the stress distribution and significantly contribute to complex seismicity even without smaller-scale frictional heterogeneities along fault. Earthquake magnitudes show significant variability when compared to a homogeneous medium, but the log-linearity of the magnitude-frequency distribution is difficult to infer due to the limited number of earthquakes

generated in the simulations. Observations in regional and global earthquake catalogues generally show a log-linear decay of magnitude with increasing number of earthquakes, in agreement with the Gutenberg-Richter distribution. However, large earthquakes along individual faults or fault sections deviate from this behavior, showing a relatively elevated number of characteristic earthquakes (Parsons et al., 2018; Schwartz & Coppersmith, 1984; Wesnousky, 1994) that follow a Gaussian distribution in addition to smaller earthquakes adhering to the Gutenberg-Richter distribution. This characteristic distribution is used as a basis for rupture forecast models (e.g., Field et al., 2017). We have combined the earthquakes from multiple simulations to emulate a regional catalogue where we may have multiple faults with different fault zone characteristics, but we ignore the interactions between these faults. In order to reproduce a Gutenberg-Richter distribution, more complexities in the model are required. One way to reproduce the log-linearity of the Gutenberg-Richter distribution would be to reduce the nucleation size in relation to the width of the velocity-weakening region. The question still remains whether frictional heterogeneities only, or additional material heterogeneities in combination with frictional heterogeneities and stress heterogeneities emulate the Gutenberg-Richter behavior in nature. The current model is an idealized approximation of the material effects of fault damage zones with small fractures. More realistic approximations would include the incorporation of viscoelastic and plasticity effects (Allison & Dunham, 2018; Erickson et al., 2017), variable pore pressure effects with depth, and time-dependent frictional parameters and initial stresses. Despite these approximations, our models provide a physical description of the effects of material heterogeneities on the long-term behavior of strike-slip faults.

Our future work will be directed toward understanding the effect of fault damage zone evolution through multiple seismic cycles. Paleoseismic studies of large strike-slip earthquakes, limited to the past 1,000–1,200 yr, suggest that the recurrence of large events is nonuniform, possibly even chaotic, with large gap in seismic activity followed by multiple seismic episodes (Grant & Sieh, 1992; Fumal et al., 2002; Seitz et al., 1997; Toké et al., 2006). A time-dependent stressing history, possibly driven by the evolution of the fault damage zone through multiple seismic episodes and aseismic creep, may better explain the observed nonniform recurrence intervals along mature faults. Previous experiments and observations (Peng & Ben-Zion, 2006; Stanchits et al., 2006) have shown that the damage can be enhanced during seismic episodes and be healed during interseismic periods. The amount and localization of damage depends on the earthquake sizes, the interseismic duration for which the fault is allowed to heal, and recurrence intervals of large earthquakes (Vidale & Li, 2003; Yang, 2015). Incorporating the evolution of fault damage zone would provide more realistic outlook on long-term structural evolution and source characteristics of mature strike-slip faults.

Appendix A: Numerical Convergence in the Simulations

We perform numerical convergence tests for the simulations with a narrow fault damage zone extending throughout the model domain. The half-width of the fault damage zone is 150 m, and the shear wave velocity reduction is 40%. We use an average node spacing of 10, 20, and 40 m. The comparison between the peak slip rate and the differential slip for a large earthquake is shown in Figure A1. The comparison of peak slip rate for simulations with different node spacings demonstrates that the onset of earthquakes are the same for the

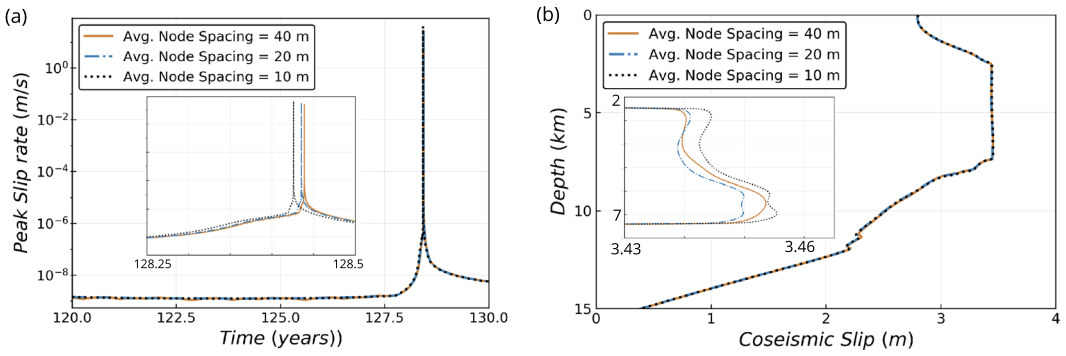

Figure A1. (a) Peak slip rate shown for multiple node spacings. (b) Differential slip of one earthquake shown for multiple node spacings.

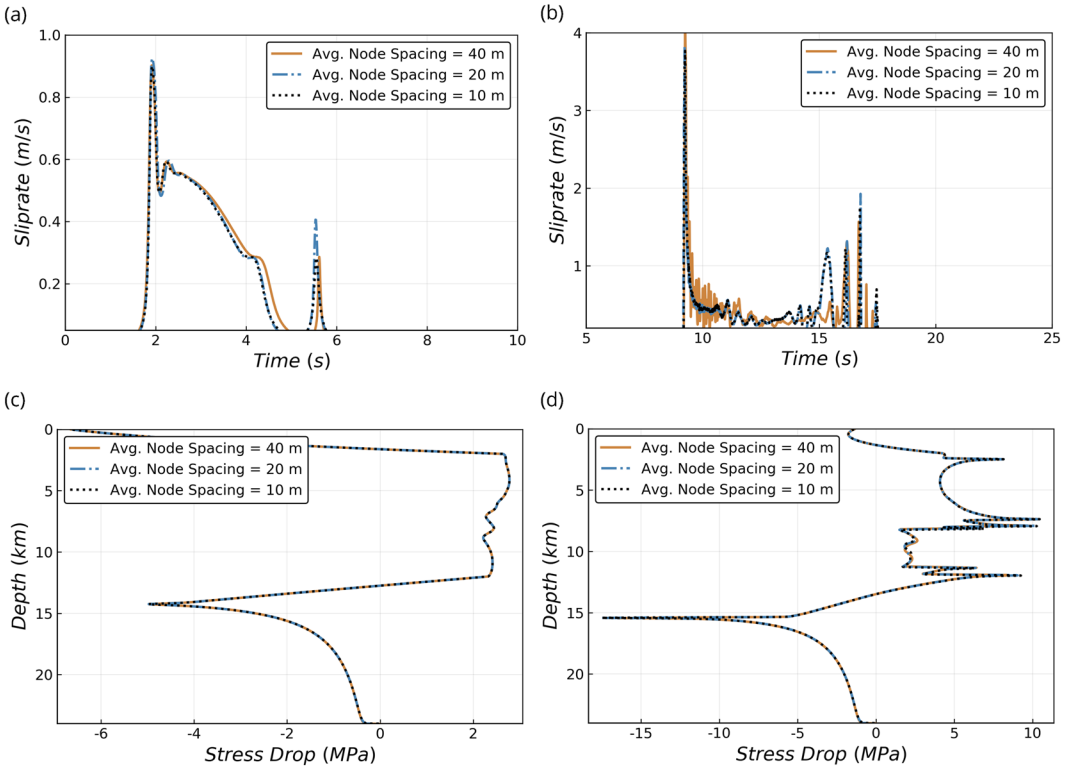

Figure A2. (a, b) Resolution tests showing the slip rate function for (a) first and (b) fifth events at 7 km depth. (c, d) The stress drop along depth of the fault for (c) first and (d) fifth events shown for multiple node spacings.

different node spacings. Furthermore, Figure A1b shows that the differential slip for different node spacings are the same, implying that the earthquake size is independent of mesh size. The shape of the differential slip shown in the inset zoom figure (Figure A1b) suggests all the features are not preserved for an average node spacing of 40 m, but they are preserved for all the other node spacings. We also show the slip rate as a function of time for the first and the fifth rupture to illustrate the comparable timing of the dynamic rupture in Figures A2a and A2b. This figure demonstrates that while the timing of dynamic rupture is comparable for all the node spacings, the node spacing of 40m shows numerical oscillations whereas the 20 and 10 m node spacings are adequately resolved. Figures A2c and A2d show the stress drops for the first and the fifth event along depth, and it is well resolved for all the node spacings. Based on this convergence study, we have chosen an average node spacing of 20 m for our study.

Data Availability Statement

The code used to perform the numerical simulations is available on zenodo (https://zenodo.org/record/3665727). GMT (Wessel et al., 2013) was used to create some figures.

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